

# **Proper Platinum Resistance Thermometer Calibration Uncertainty Analysis**

# Introduction

- Uncertainty quantification is a primary task of the metrologist
- The uncertainty analysis must reflect our best understanding of the measurement and the instrument being calibrated
- If a calibration process is not fully understood, the uncertainty analysis is almost certainly flawed
- If the uncertainties do not reflect some aspects of UUT behavior, it will not reflect the UUT in use

# Introduction

- Incomplete uncertainty analysis
  - Thorough uncertainty analysis is often more complex than it appears
  - Ignorance is bliss - the less we know, the better our numbers look
  - Although our assessors are very good, some do not possess sufficient *current* understanding to notice omissions in the uncertainty analysis

- Philosophical viewpoint
  - Should the calibration be considered as an isolated experiment or as part of a process?
  - Should the uncertainty analysis include only those components present at the time of calibration?
  - Should the uncertainty analysis include additional components to reflect UUT short term behavior?
  - Should the uncertainty analysis include additional components to reflect UUT long term behavior?

# Introduction

- Consequently, it is easy to underestimate the real measurement uncertainty
  - Some omissions are insignificant to the final result and amount to a minor embarrassment or controversy when discovered
  - Other omissions may result in a noticeable, substantive underestimation of the final uncertainty

# Categorization

- Often categorization helps us see things more clearly
- Platinum resistance thermometer calibration uncertainties can be categorized into two areas:
- Uncertainties in temperature
- Uncertainties in resistance measurement

# Categorization

- Thermal uncertainties
  - Temperature stability
  - Temperature uniformity
  - Determination of the temperature
  - Temperature equilibrium
  - Self heating caused by excitation current\*
- Resistance measurement uncertainties
  - Readout accuracy
  - Readout linearity
  - Electrical noise
  - Electrical interference
  - Self heating caused by excitation current\*

\*Evaluate only once (avoid double counting)

# Uncertainty Budget

## Uncertainty Evaluation

Type A Evaluation	Category	LN2 mK	tn100 mK	Hg mK	TPW mK	FPIn mK	FPSn mK	FPZn mK	t500 mK
Readout Noise (1σ)	E	0.20	0.20	0.20	0.20	0.20	0.20	0.20	0.20
<b>Total A</b>	<b>A</b>	<b>0.20</b>							
<b>Type B Evaluation</b>									
SPRT accuracy (calibration and drift)	T	1.50	1.50	1.25	0.80	1.45	1.50	1.75	2.50
Bath uniformity	T	1.15	0.58	0.58	0.58	0.87	1.15	1.44	1.73
Thermometer readout (6 ppm, SPRT)	E	0.20	0.21	0.22	0.22	0.36	0.44	0.64	0.75
Thermometer readout (6 ppm, UUT)	E	0.03	0.08	0.11	0.84	0.24	0.29	0.42	0.54
<b>Total B</b>	<b>B</b>	<b>1.91</b>	<b>1.63</b>	<b>1.42</b>	<b>1.45</b>	<b>1.79</b>	<b>2.03</b>	<b>2.50</b>	<b>3.31</b>
Total Standard Uncertainty	U	1.92	1.65	1.43	1.46	1.80	2.04	2.51	3.31
<b>Total Expanded Uncertainty (<math>k=2</math>)</b>	<b>U'</b>	<b>3.84</b>	<b>3.29</b>	<b>2.87</b>	<b>2.93</b>	<b>3.60</b>	<b>4.08</b>	<b>5.02</b>	<b>6.62</b>

# Additional Components

- Some components are missing
  - Reference SPRT  $R_{TPW}$  propagation
  - Reference SPRT self heating correction
  - **Reference SPRT immersion error**
  - **UUT noise contribution**
  - UUT short term repeatability
  - UUT immersion error
  - UUT insulation resistance
  - **Mathematical model uncertainties**
  - Process repeatability

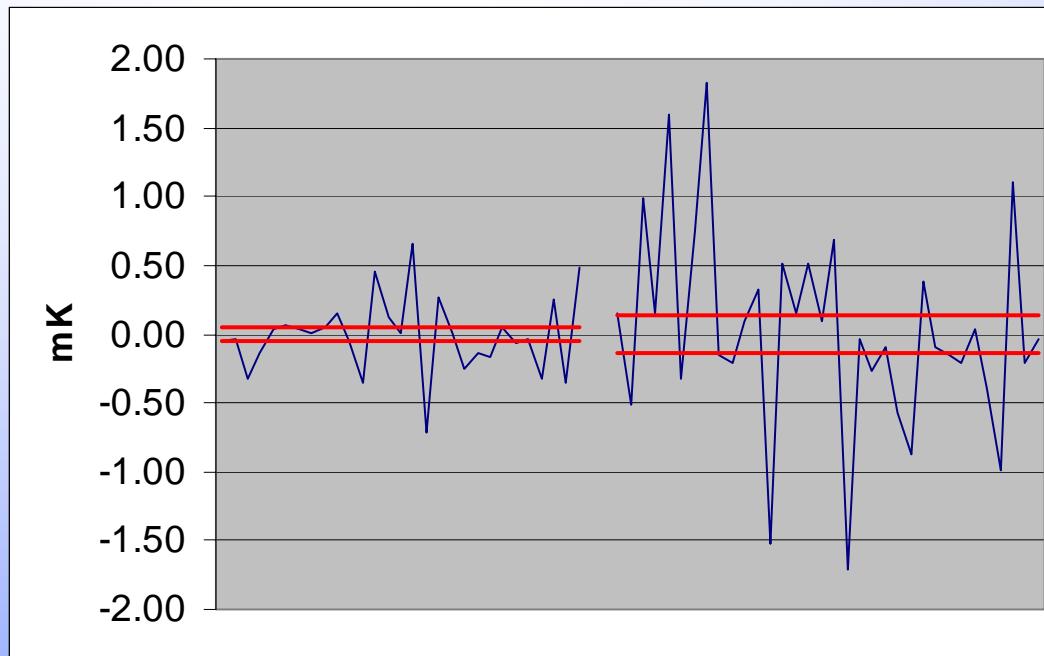
# SPRT Uncertainties

- SPRT  $R_{TPW}$  measurement (or ambiguity allowance) during use propagates to uncertainty in determination of  $W_{T90}$ 
  - Example,  $R_{TPW}$  uncertainty of 0.5 mK becomes 1.4 mK at 500 °C
- SPRT self heating is different in different thermal environments
  - Fixed point cells (SPRT cal) and comparison baths (use)
- SPRT has immersion requirements which may or may not be satisfied in the application
  - For example, calibration of short sensors

# UUT Uncertainties

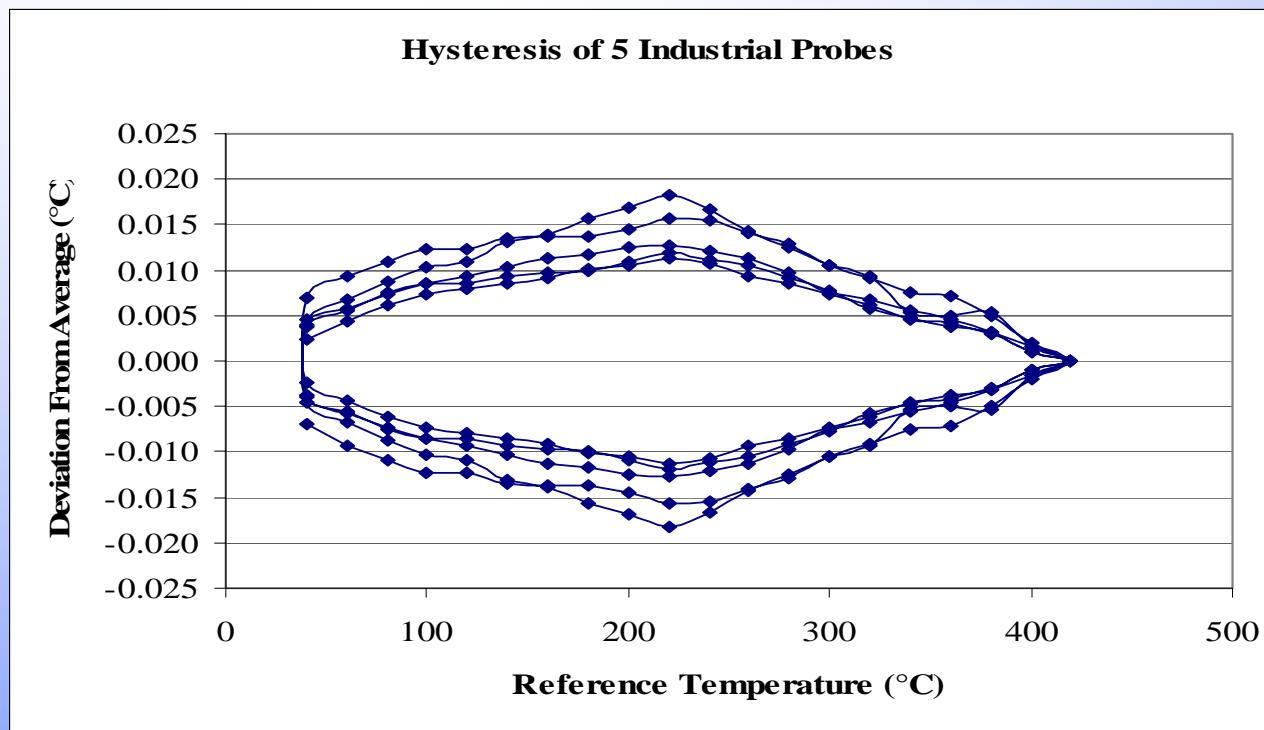
- UUT noise allowance

- The noise influences the precision of the average obtained during the calibration



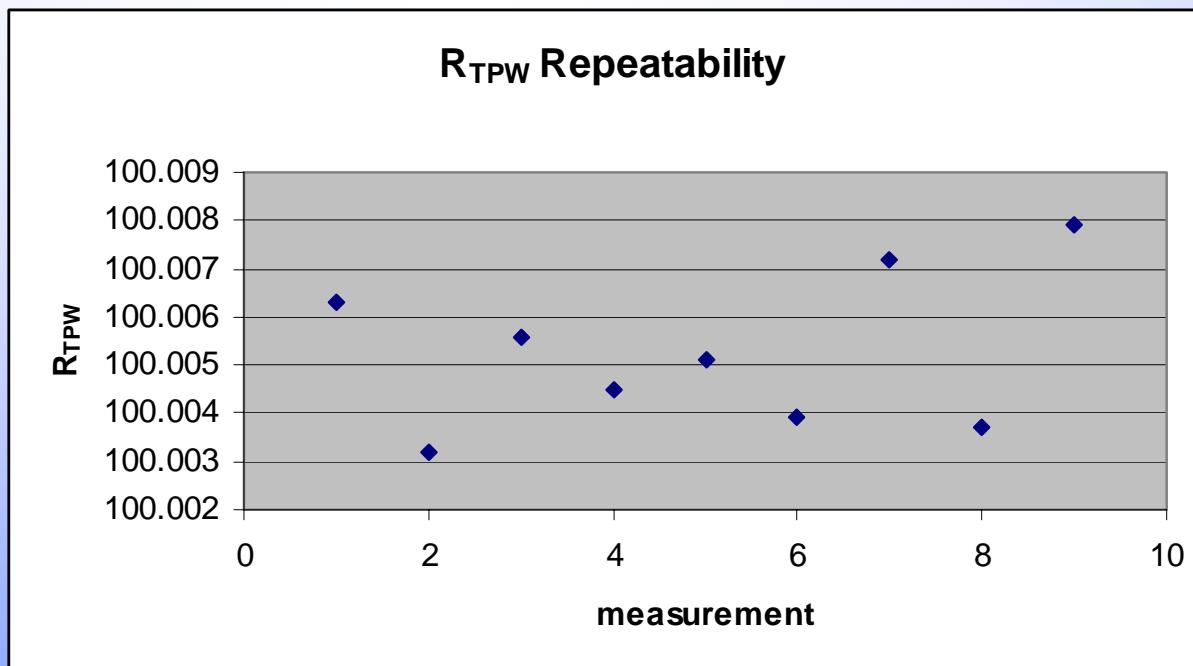
# UUT Uncertainties

- UUT short term repeatability
  - Hysteresis



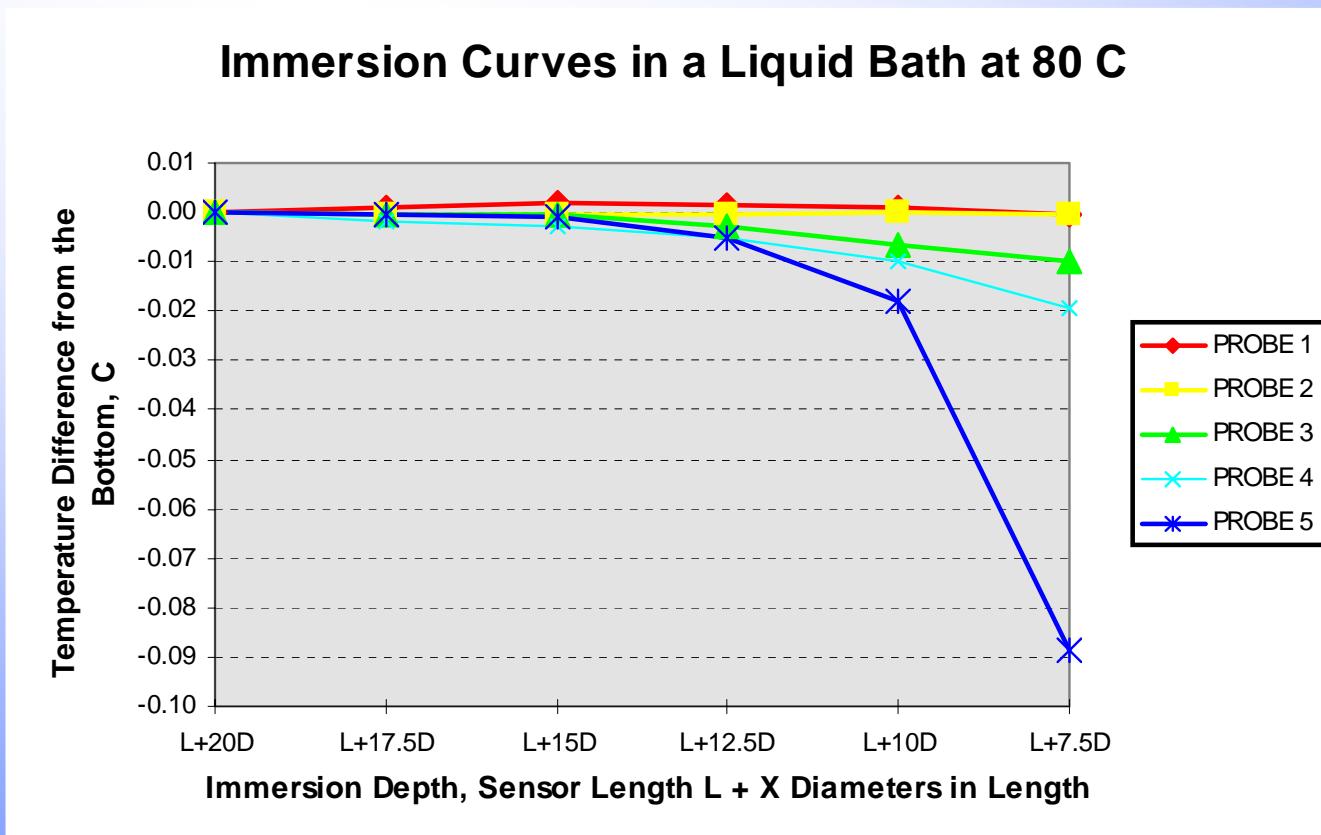
# UUT Uncertainties

- UUT short term repeatability
  - $R_{TPW}$  repeatability (average = 100.0053, spread = 0.012 °C)



# UUT Uncertainties

- UUT immersion error



# UUT Uncertainties

- UUT insulation resistance effects (worst case)

$$1) \quad R_{total}(\Omega) = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}} = \frac{1}{\frac{1}{256\Omega} + \frac{1}{10M\Omega}}$$

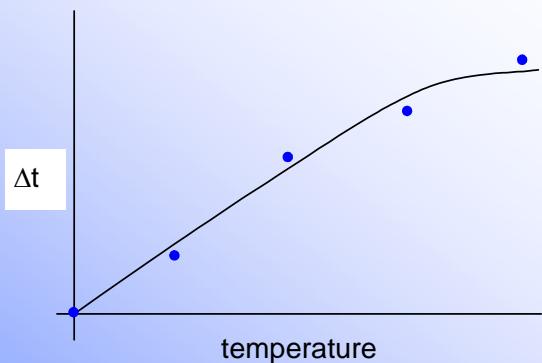
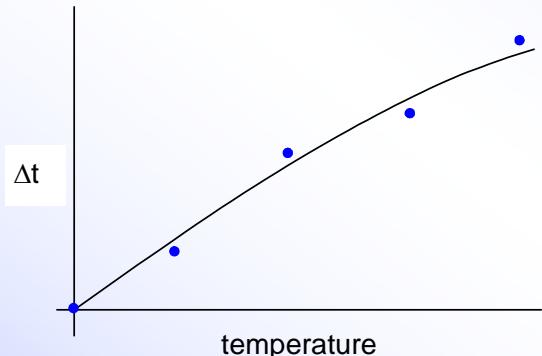
$$2) \quad R_{total}(\Omega) = 255.993447 \Omega$$

$$3) \quad \Delta R = 256\Omega - 255.993447 \Omega \approx 6.55 \times 10^{-3} \Omega$$

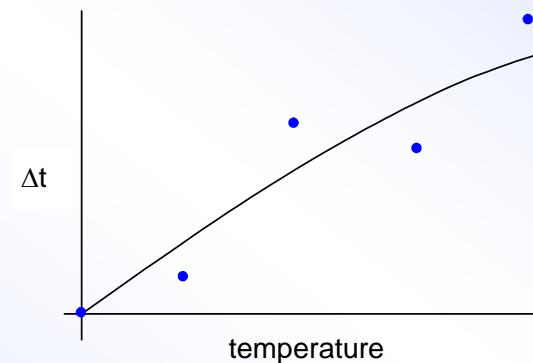
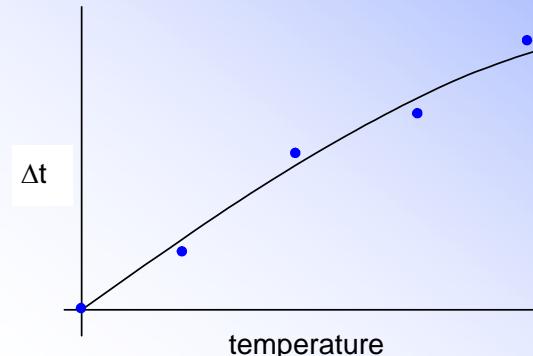
$$4) \quad 6.55 \times 10^{-3} \Omega \Big/ 0.36\%_C = 1.82 \times 10^{-3} \Omega \approx 18.2mK$$

$$5) \quad 18.2mK \Big/ \sqrt{3} = 10.5mK$$

# Mathematical Model U

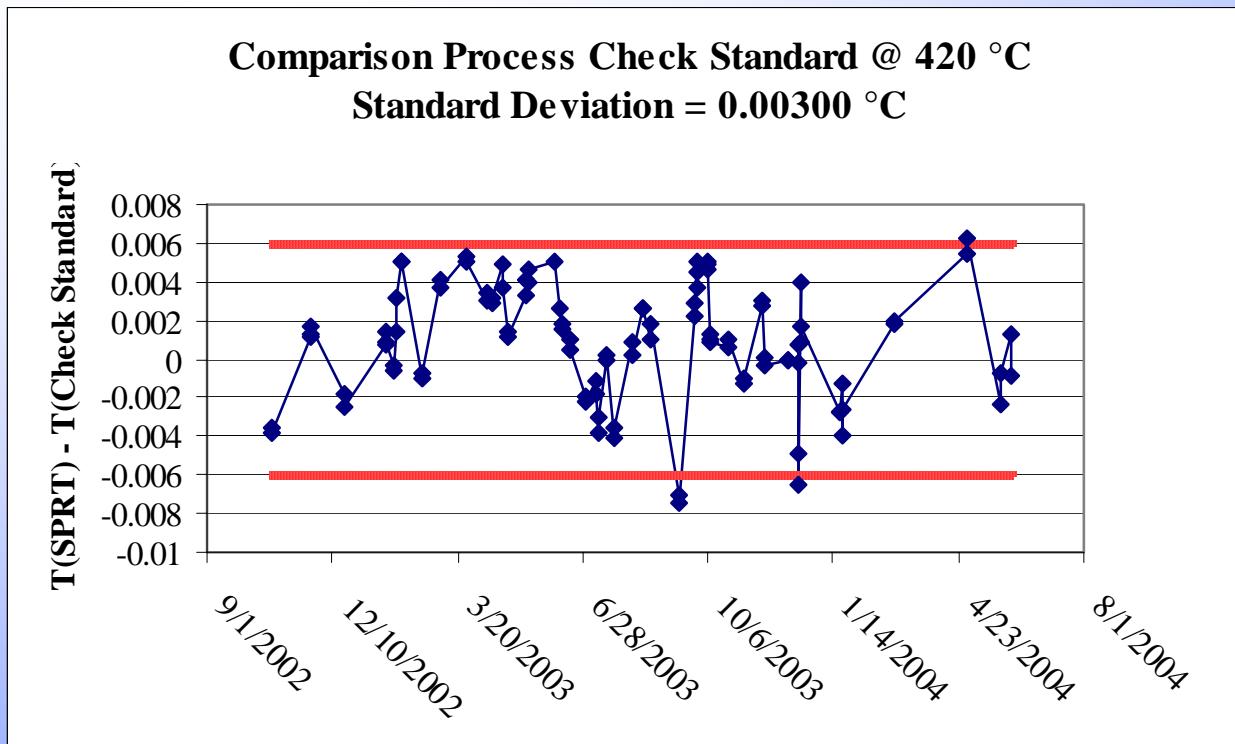


Curve Fit



Magnitude of Residuals

# Process Repeatability



# Revised Uncertainty Budget

## Uncertainty Evaluation

Type A Evaluation	Category	LN2 mK	tn100 mK	Hg mK	TPW mK	FPIn mK	FPSn mK	FPZn mK	t500 mK
Process variability	P	0.90	1.80	1.30	1.00	1.99	2.60	3.20	3.70
Precision of UUT measurement	T&E	2.22	1.67	1.67	1.11	1.67	1.67	2.22	2.78
Propagated repeatability of R <sub>TPW</sub> (UUT)	UUT	0.42	1.36	1.94	2.31	3.72	4.36	5.91	6.47
<b>Total A</b>	<b>A</b>	<b>2.43</b>	<b>2.81</b>	<b>2.87</b>	<b>2.75</b>	<b>4.53</b>	<b>5.35</b>	<b>7.08</b>	<b>7.95</b>
Type B Evaluation									
SPRT accuracy (calibration and drift)	T	1.50	1.50	1.25	0.80	1.45	1.50	1.75	2.50
SPRT R <sub>TPW</sub> propagation	T	0.05	0.17	0.24	0.29	0.55	0.55	0.74	0.81
SPRT self heating correction	T	0.58	0.58	0.58	0.58	0.58	0.58	0.58	0.58
Insulation resistance (UUT)		0.01	0.09	0.20	0.29	0.75	1.03	2.10	2.61
Bath uniformity	T	1.15	0.58	0.58	0.58	0.87	1.15	1.44	1.73
Thermometer readout (6 ppm, SPRT)	E	0.20	0.21	0.22	0.22	0.36	0.44	0.64	0.75
Thermometer readout (6 ppm, UUT)	E	0.03	0.08	0.11	0.84	0.24	0.29	0.42	0.54
<b>Total B</b>	<b>B</b>	<b>1.99</b>	<b>1.74</b>	<b>1.56</b>	<b>1.61</b>	<b>2.10</b>	<b>2.41</b>	<b>3.40</b>	<b>4.32</b>
Total Standard Uncertainty	U	3.15	3.30	3.27	3.19	5.00	5.86	7.85	9.05
<b>Total Expanded Uncertainty (<i>k</i>=2)</b>	<b>U'</b>	<b>6.29</b>	<b>6.61</b>	<b>6.54</b>	<b>6.38</b>	<b>9.99</b>	<b>11.73</b>	<b>15.71</b>	<b>18.10</b>

# Difference

Original Uncertainty Evaluation	U'	3.84	3.29	2.87	2.93	3.60	4.08	5.02	6.62
Revised Uncertainty Evaluation	U'	6.29	6.61	6.54	6.38	9.99	11.73	15.71	18.10
Difference	Absolute	2.46	3.31	3.67	3.45	6.39	7.65	10.69	11.48
	%	64.0	100.6	128.1	117.7	177.4	187.7	213.1	173.3

# Conclusions

- Uncertainty evaluation involves variables that may not be readily apparent
- Some variables are difficult to quantify and may vary from UUT to UUT
- Underestimating the uncertainties in this manner may lead to significant errors
- Incomplete uncertainty analyses are very common among both unaccredited and accredited laboratories