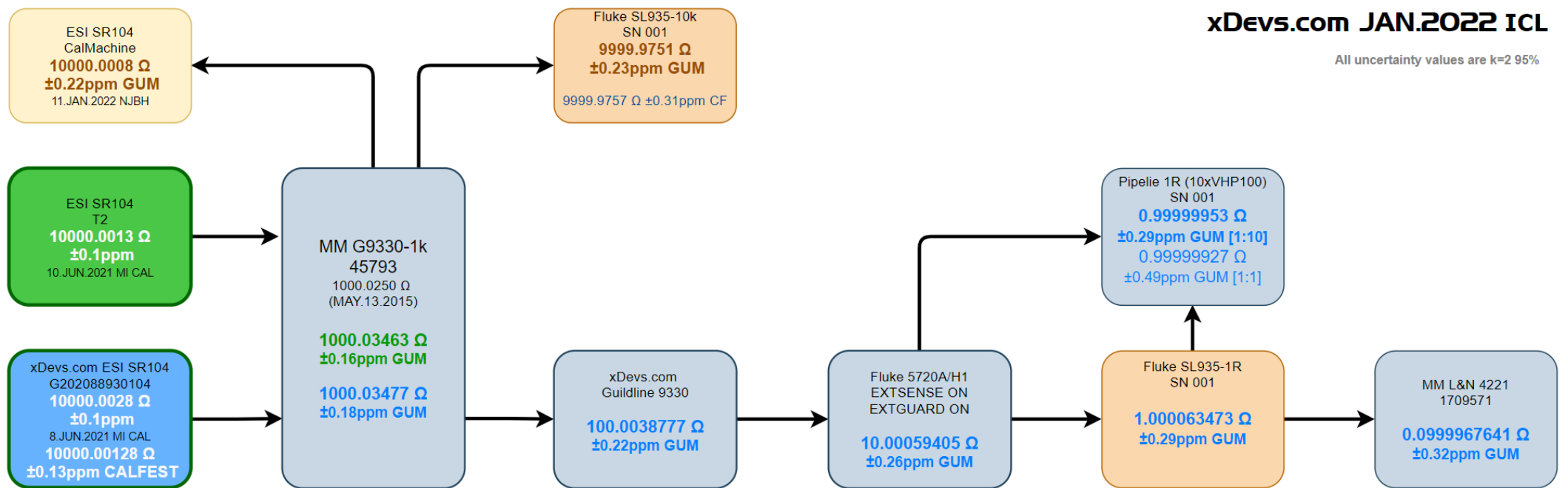


Transfers with resistance standards at xDevs.com NJBH Lab

xDevs.com JAN.2022 ICL

All uncertainty values are k=2 95%



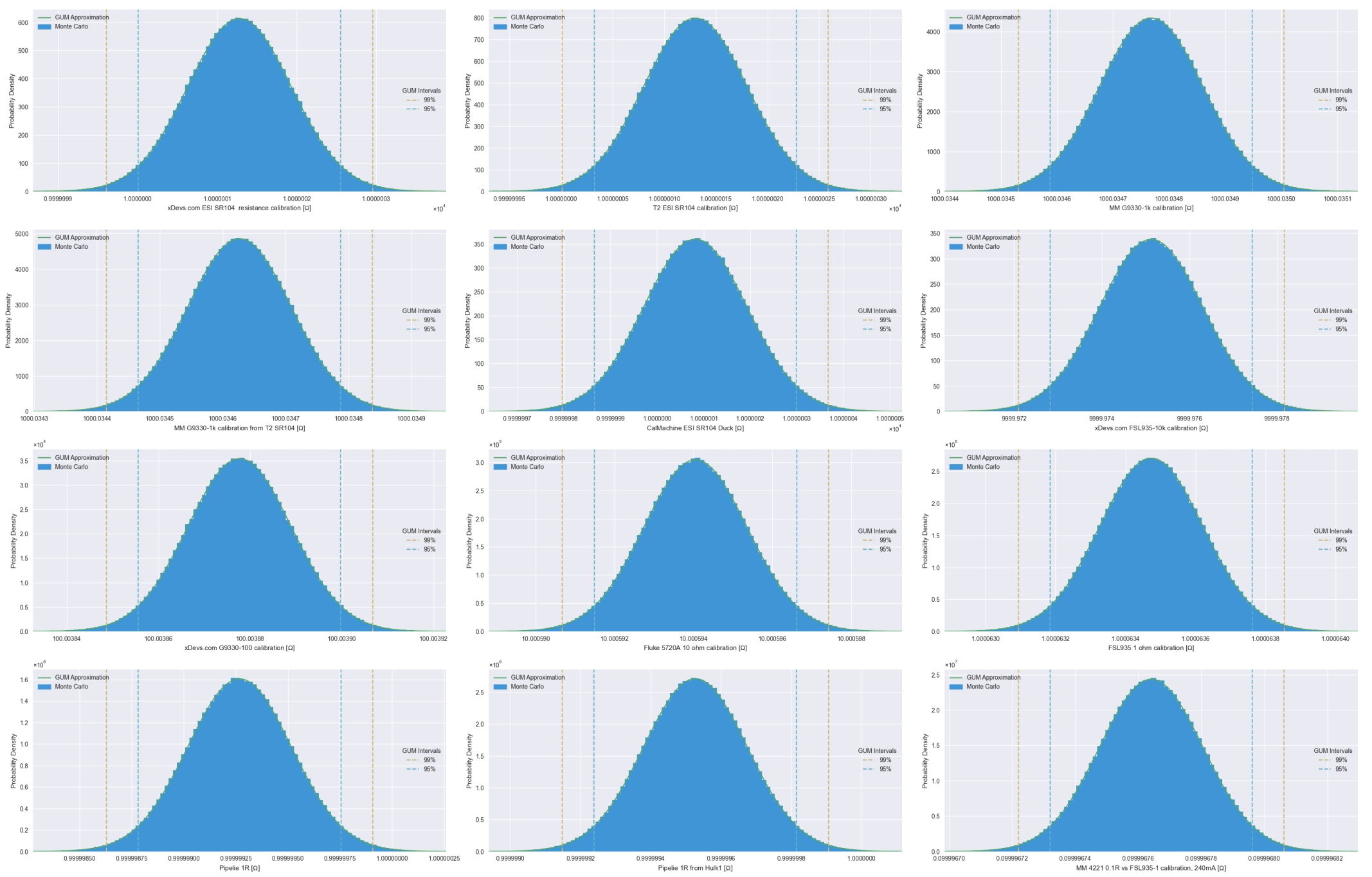
Summary and result analysis

All measurements performed with Measurements International Model 6010B Automatic Resistance Bridge, using DCC technology.

With exception of Fluke 5720A/H1 all measurement devices and standards were thermally stabilized in peltier active thermal chamber.

Temperature of measurement was set at +23.0 °C ±0.2°C . No corrections for thermal coefficients was applied in this report.

| Function | Method | Nominal | Std. Uncertainty | 95% Coverage | k | Deg. Freedom |
|----------------|-------------|---------------|------------------|--------------------------------|-------|---------------|
| R_{REF} | GUM | 10000.00128 Ω | 0.00065 Ω | ± 0.0013 Ω | 1.960 | inf |
| R_{REF} | Monte Carlo | 10000.00128 Ω | 0.00065 Ω | (10000.00000 Ω, 10000.00255 Ω) | 1.962 | - |
| R_{REF2} | GUM | 10000.0013 Ω | 0.00050 Ω | ± 0.00098 Ω | 1.960 | inf |
| R_{REF2} | Monte Carlo | 10000.0013 Ω | 0.00050 Ω | (10000.00032 Ω, 10000.00228 Ω) | 1.960 | - |
| R_{1k} | GUM | 1000.034768 Ω | 0.000092 Ω | ± 0.00018 Ω | 1.960 | 1305544786.3 |
| R_{1k} | Monte Carlo | 1000.034768 Ω | 0.000092 Ω | (1000.034587 Ω, 1000.034949 Ω) | 1.962 | - |
| R_{1kT2} | GUM | 1000.034627 Ω | 0.000082 Ω | ± 0.00016 Ω | 1.960 | inf |
| R_{1kT2} | Monte Carlo | 1000.034627 Ω | 0.000082 Ω | (1000.034466 Ω, 1000.034787 Ω) | 1.959 | - |
| R_{CMDUCK} | GUM | 10000.0008 Ω | 0.0011 Ω | ± 0.0022 Ω | 1.960 | 122538273.4 |
| R_{CMDUCK} | Monte Carlo | 10000.0008 Ω | 0.0011 Ω | (9999.9986 Ω, 10000.0030 Ω) | 1.959 | - |
| R_{FSL10k} | GUM | 9999.9751 Ω | 0.0012 Ω | ± 0.0023 Ω | 1.960 | 56585304516.7 |
| R_{FSL10k} | Monte Carlo | 9999.9751 Ω | 0.0012 Ω | (9999.9728 Ω, 9999.9774 Ω) | 1.959 | - |
| R_{100} | GUM | 100.003878 Ω | 0.000011 Ω | ± 0.000022 Ω | 1.960 | 2408282652.1 |
| R_{100} | Monte Carlo | 100.003878 Ω | 0.000011 Ω | (100.003856 Ω, 100.003900 Ω) | 1.959 | - |
| R_{10} | GUM | 10.0005941 Ω | 1.3e-06 Ω | ± 2.6e-06 Ω | 1.960 | 25179230.3 |
| R_{10} | Monte Carlo | 10.0005940 Ω | 1.3e-06 Ω | (10.0005915 Ω, 10.0005966 Ω) | 1.961 | - |
| R_{FSL935} | GUM | 1.00006347 Ω | 1.5e-07 Ω | ± 2.9e-07 Ω | 1.960 | 7785363.5 |
| R_{FSL935} | Monte Carlo | 1.00006347 Ω | 1.5e-07 Ω | (1.00006318 Ω, 1.00006376 Ω) | 1.960 | - |
| R_{PP} | GUM | 0.99999927 Ω | 2.5e-07 Ω | ± 4.9e-07 Ω | 1.960 | 8444.6 |
| R_{PP} | Monte Carlo | 0.99999927 Ω | 2.5e-07 Ω | (0.99999878 Ω, 0.99999975 Ω) | 1.959 | - |
| R_{PPH1} | GUM | 0.99999953 Ω | 1.5e-07 Ω | ± 2.9e-07 Ω | 1.960 | 27454495.0 |
| R_{PPH1} | Monte Carlo | 0.99999953 Ω | 1.5e-07 Ω | (0.99999924 Ω, 0.99999982 Ω) | 1.962 | - |
| $R_{MMLN4221}$ | GUM | 0.099996764 Ω | 1.6e-08 Ω | ± 3.2e-08 Ω | 1.960 | 2966862.0 |
| $R_{MMLN4221}$ | Monte Carlo | 0.099996764 Ω | 1.6e-08 Ω | (0.099996732 Ω, 0.099996796 Ω) | 1.962 | - |



Standardized Input Values

| Variable | Mean | Std. Uncertainty | Deg. Freedom | Description |
|---------------------------|-------------|------------------|--------------|--|
| R | 10000.00128 | 0.00065 Ω | inf | xDevs.com SR104 from Calfest |
| R ₂ | 10000.00130 | 0.00050 Ω | inf | T2 ESI SR104 from MI CAL |
| ratio | 9.99965361 | 6.5e-07 | 3.3e+08 | DCC Ratio to MMG9330-1k |
| ratio ₂ | 9.99965505 | 6.5e-07 | inf | DCC Ratio to MMG9330-1k, T2 value |
| ratio ₁₀ | 9.99979373 | 6.7e-07 | 1.7e+06 | Hulk1 5720A |
| ratio ₁₀₀ | 9.99995991 | 6.5e-07 | 1.5e+09 | DCC Ratio to xDevs.com 100 R |
| ratio _{cm} | 9.99965386 | 9.2e-07 | 5.9e+07 | DCC ratio for CM Duck |
| ratio _{fsl} | 9.99995932 | 6.8e-07 | 4.3e+05 | FSL935 from H1-10 |
| ratio _{fsl10k} | 9.9996282 | 1.0e-06 | inf | DCC ratio for FSL935-10k |
| ratio _{mmln4221} | 10.00095835 | 7.1e-07 | 1.4e+05 | DCC ratio for MM LN4221 0.1R, +23.12°C |
| ratio _{pp} | 0.99993580 | 2.0e-07 | 3500 | DCC ratio of PP to FSL935 |
| ratio _{pph1} | 10.00059878 | 6.7e-07 | 3.7e+06 | DCC ratio from Hulk1 10R to PP1R |

Uncertainty Budget

| Variable | Component | Description | Standard Uncertainty | Deg. Freedom |
|----------------|-----------|------------------------------|----------------------|--------------|
| R | - | xDevs.com SR104 from Calfest | 0.00065 Ω | inf |
| - | u(R) | Calibrated OCT/2021 | 0.00065 Ω | inf |
| R ₂ | - | T2 ESI SR104 from MI CAL | 0.00050 Ω | inf |
| - | u(R2) | Calibrated JUN/2021 | 0.00050 Ω | inf |
| ratio | - | DCC Ratio to MMG9330-1k | 6.5e-07 | 327104479.7 |

| Variable | Component | Description | Standard Uncertainty | Deg. Freedom |
|---------------------------|--------------------------------|--|----------------------|--------------|
| - | u(ratio) | XFER to 1000 Ohm | 3.1e-08 | 1579.0 |
| - | u1(ratio) | SR104 U | 6.5e-07 | inf |
| ratio ₂ | - | DCC Ratio to MMG9330-1k, T2 value | 6.5e-07 | inf |
| - | u(ratio2) | XFER to 1000 Ohm T2 | 4.0e-08 | inf |
| - | u1(ratio2) | SR104 T2 U | 6.5e-07 | inf |
| ratio ₁₀ | - | Hulk1 5720A | 6.7e-07 | 1710039.5 |
| - | u(ratio ₁₀) | XFER to 10 ohm | 1.5e-07 | 4096.0 |
| - | u1(ratio ₁₀) | XFER 100 | 2.7e-08 | inf |
| - | u2(ratio ₁₀) | XFER 1k | 3.1e-08 | 1579.0 |
| - | u3(ratio ₁₀) | SR104 U | 6.5e-07 | inf |
| ratio ₁₀₀ | - | DCC Ratio to xDevs.com 100 R | 6.5e-07 | 1478418900.8 |
| - | u(ratio ₁₀₀) | XFER to 100 | 2.7e-08 | 4096.0 |
| - | u1(ratio ₁₀₀) | XFER to 1k | 3.1e-08 | inf |
| - | u2(ratio ₁₀₀) | SR104 U | 6.5e-07 | inf |
| ratio _{cm} | - | DCC ratio for CM Duck | 9.2e-07 | 58567283.2 |
| - | u(ratio _{cm}) | XFER 1k | 4.8e-08 | 436.0 |
| - | u1(ratio _{cm}) | SR104 U T2 | 6.5e-07 | inf |
| - | u2(ratio _{cm}) | SR104 U | 6.5e-07 | inf |
| ratio _{fsl} | - | FSL935 from H1-10 | 6.8e-07 | 428179.5 |
| - | u(ratio _{fsl}) | XFER 1R | 1.1e-07 | 305.0 |
| - | u1(ratio _{fsl}) | XFER 10 | 1.5e-07 | inf |
| - | u2(ratio _{fsl}) | XFER 100 | 2.7e-08 | 4096.0 |
| - | u3(ratio _{fsl}) | XFER 1k | 3.1e-08 | inf |
| - | u4(ratio _{fsl}) | SR104 U | 6.5e-07 | inf |
| ratio _{fsl10k} | - | DCC ratio for FSL935-10k | 1.0e-06 | inf |
| - | u(ratio _{fsl10k}) | XFER 10k FSL | 4.1e-07 | inf |
| - | u1(ratio _{fsl10k}) | SR104 U | 6.5e-07 | inf |
| - | u2(ratio _{fsl10k}) | SR104 U T2 | 6.5e-07 | inf |
| ratio _{mmln4221} | - | DCC ratio for MM LN4221 0.1R, +23.12°C | 7.1e-07 | 141825.7 |
| - | u(ratio _{mmln4221}) | XFER 1R | 2.3e-07 | 1616.0 |
| - | u1(ratio _{mmln4221}) | XFER 10R | 1.5e-07 | inf |
| - | u2(ratio _{mmln4221}) | XFER 100R | 2.7e-08 | inf |
| - | u3(ratio _{mmln4221}) | XFER 1k | 3.1e-08 | inf |
| - | u4(ratio _{mmln4221}) | SR104 U | 6.5e-07 | inf |
| - | u5(ratio _{mmln4221}) | XFER 0.1R | 8.7e-08 | inf |
| ratio _{pp} | - | DCC ratio of PP to FSL935 | 2.0e-07 | 3537.6 |
| - | u(ratio _{pp}) | XFER PP1R | 4.5e-09 | 3525.0 |
| - | u1(ratio _{pp}) | XFER FSL1 | 1.1e-07 | 333.0 |
| - | u2(ratio _{pp}) | Hulk 10r | 1.5e-07 | inf |
| - | u3(ratio _{pp}) | XFER 100 | 2.7e-08 | 4096.0 |
| - | u4(ratio _{pp}) | XFER 1k | 3.1e-08 | 1579.0 |
| - | u5(ratio _{pp}) | SR104 U | 6.5e-08 | inf |
| ratio _{pph1} | - | DCC ratio from Hulk1 10R to PP1R | 6.7e-07 | 3740928.9 |

| Variable | Component | Description | Standard Uncertainty | Deg. Freedom |
|----------|----------------------------|-------------|----------------------|--------------|
| - | u1(ratio _p ph1) | pp1h | 4.2e-08 | 60.0 |
| - | u2(ratio _p ph1) | 10 | 1.5e-07 | inf |
| - | u3(ratio _p ph1) | 100 | 2.7e-08 | 4096.0 |
| - | u4(ratio _p ph1) | 1k | 3.1e-08 | 1579.0 |
| - | u5(ratio _p ph1) | SR104U | 6.5e-07 | inf |

Sensitivity Coefficients

R_REF_

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 1.0 | 100.00% | 1.00 | 100.00% |
| R ₂ | 0.0 | 0.00% | 2.9e-08 | 0.00% |
| ratio | 0.0 | 0.00% | 0.000022 Ω | 0.00% |
| ratio ₂ | 0.0 | 0.00% | 0.000022 Ω | 0.00% |
| ratio ₁₀ | 0.0 | 0.00% | 0.000022 Ω | 0.00% |
| ratio ₁₀₀ | 0.0 | 0.00% | 0.000022 Ω | 0.00% |
| ratio _{cm} | 0.0 | 0.00% | 0.000016 Ω | 0.00% |
| ratio _{fsl} | 0.0 | 0.00% | 0.000021 Ω | 0.00% |
| ratio _{fsl10k} | 0.0 | 0.00% | 0.000014 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 0.000020 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 0.000073 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 0.000022 Ω | 0.00% |

R_REF2

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.0 | 0.00% | 2.0e-08 | 0.00% |
| R ₂ | 1.0 | 100.00% | 1.0 | 100.00% |
| ratio | 0.0 | 0.00% | 0.000020 Ω | 0.00% |
| ratio ₂ | 0.0 | 0.00% | 0.000020 Ω | 0.00% |
| ratio ₁₀ | 0.0 | 0.00% | 0.000019 Ω | 0.00% |
| ratio ₁₀₀ | 0.0 | 0.00% | 0.000020 Ω | 0.00% |
| ratio _{cm} | 0.0 | 0.00% | 0.000014 Ω | 0.00% |
| ratio _{fsl} | 0.0 | 0.00% | 0.000019 Ω | 0.00% |
| ratio _{fsl10k} | 0.0 | 0.00% | 0.000013 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 0.000018 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 0.000064 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 0.000019 Ω | 0.00% |

R_1k

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|----------|-----------------|----------------|----------------|---------------|
| R | 0.10 | 49.95% | 0.100 | 49.73% |

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R ₂ | 0.0 | 0.00% | 3.2e-09 | 0.00% |
| ratio | -100.0 Ω | 50.05% | 100.2 Ω | 50.05% |
| ratio ₂ | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |
| ratio ₁₀ | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |
| ratio ₁₀₀ | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |
| ratio _{cm} | 0.0 | 0.00% | 1.7e-06 Ω | 0.00% |
| ratio _{fsl} | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |
| ratio _{fsl10k} | 0.0 | 0.00% | 1.6e-06 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 2.2e-06 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 8.0e-06 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |

R_1k_T2

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.0 | 0.00% | 2.4e-09 | 0.00% |
| R ₂ | 0.10 | 37.09% | 0.10 | 37.13% |
| ratio | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |
| ratio ₂ | -100.0 Ω | 62.91% | 100.0 Ω | 62.82% |
| ratio ₁₀ | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |
| ratio ₁₀₀ | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |
| ratio _{cm} | 0.0 | 0.00% | 1.7e-06 Ω | 0.00% |
| ratio _{fsl} | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |
| ratio _{fsl10k} | 0.0 | 0.00% | 1.6e-06 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 2.2e-06 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 8.0e-06 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 2.4e-06 Ω | 0.00% |

R_CMDUCK

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.50 | 8.61% | 0.50 | 8.58% |
| R ₂ | 0.50 | 5.09% | 0.50 | 5.09% |
| ratio | -500.0 Ω | 8.63% | 500.8 Ω | 8.64% |
| ratio ₂ | -500.0 Ω | 8.64% | 499.9 Ω | 8.62% |
| ratio ₁₀ | 0.0 | 0.00% | 0.000019 Ω | 0.00% |
| ratio ₁₀₀ | 0.0 | 0.00% | 0.000020 Ω | 0.00% |
| ratio _{cm} | 1000.0 Ω | 69.04% | 1000.3 Ω | 68.93% |
| ratio _{fsl} | 0.0 | 0.00% | 0.000019 Ω | 0.00% |
| ratio _{fsl10k} | 0.0 | 0.00% | 0.000013 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 0.000018 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 0.000064 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 0.000019 Ω | 0.00% |

R_FSL10k

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.50 | 7.59% | 0.50 | 7.57% |
| R ₂ | 0.50 | 4.49% | 0.50 | 4.49% |
| ratio | -500.0 Ω | 7.60% | 500.8 Ω | 7.62% |
| ratio ₂ | -500.0 Ω | 7.62% | 499.9 Ω | 7.60% |
| ratio ₁₀ | 0.0 | 0.00% | 0.000041 Ω | 0.00% |
| ratio ₁₀₀ | 0.0 | 0.00% | 0.000042 Ω | 0.00% |
| ratio _{cm} | 0.0 | 0.00% | 0.000030 Ω | 0.00% |
| ratio _{fsl} | 0.0 | 0.00% | 0.000040 Ω | 0.00% |
| ratio _{fsl10k} | 1000.0 Ω | 72.71% | 1000.1 Ω | 72.63% |
| ratio _{mmln4221} | 0.0 | 0.00% | 0.000038 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 0.00014 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 0.000041 Ω | 0.00% |

R100

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.010 | 33.27% | 0.0100 | 33.25% |
| R ₂ | 0.0 | 0.00% | 1.7e-10 | 0.00% |
| ratio | -10.0 Ω | 33.34% | 10.0 Ω | 33.46% |
| ratio ₂ | 0.0 | 0.00% | 1.3e-07 Ω | 0.00% |
| ratio ₁₀ | 0.0 | 0.00% | 1.3e-07 Ω | 0.00% |
| ratio ₁₀₀ | -10.0 Ω | 33.39% | 10.0 Ω | 33.31% |
| ratio _{cm} | 0.0 | 0.00% | 9.3e-08 Ω | 0.00% |
| ratio _{fsl} | 0.0 | 0.00% | 1.3e-07 Ω | 0.00% |
| ratio _{fsl10k} | 0.0 | 0.00% | 8.5e-08 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 1.2e-07 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 4.3e-07 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 1.3e-07 Ω | 0.00% |

R_10

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.0010 | 24.62% | 0.00100 | 24.59% |
| R ₂ | 0.0 | 0.00% | 7.1e-12 | 0.00% |
| ratio | -1.0 Ω | 24.68% | 1.0 Ω | 24.75% |
| ratio ₂ | 0.0 | 0.00% | 5.5e-09 Ω | 0.00% |
| ratio ₁₀ | -1.0 Ω | 25.99% | 1.00 Ω | 25.94% |
| ratio ₁₀₀ | -1.0 Ω | 24.72% | 1.00 Ω | 24.64% |
| ratio _{cm} | 0.0 | 0.00% | 3.9e-09 Ω | 0.00% |
| ratio _{fsl} | 0.0 | 0.00% | 5.2e-09 Ω | 0.00% |
| ratio _{fsl10k} | 0.0 | 0.00% | 3.5e-09 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 5.0e-09 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 1.8e-08 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 5.3e-09 Ω | 0.00% |

R_FSL935

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.00010 | 19.43% | 0.000100 | 19.38% |
| R ₂ | 0.0 | 0.00% | 4.9e-12 | 0.00% |
| ratio | -0.10 Ω | 19.48% | 0.10 Ω | 19.51% |
| ratio ₂ | 0.0 | 0.00% | 3.8e-09 Ω | 0.00% |
| ratio ₁₀ | -0.10 Ω | 20.51% | 0.100 Ω | 20.44% |
| ratio ₁₀₀ | -0.10 Ω | 19.51% | 0.100 Ω | 19.42% |
| ratio _{cm} | 0.0 | 0.00% | 2.7e-09 Ω | 0.00% |
| ratio _{fsl} | -0.10 Ω | 21.07% | 0.10 Ω | 21.06% |
| ratio _{fsl10k} | 0.0 | 0.00% | 2.4e-09 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 3.4e-09 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 1.2e-08 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 3.7e-09 Ω | 0.00% |

R_PP

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.000100 | 6.86% | 0.000100 | 6.86% |
| R ₂ | 0.0 | 0.00% | 4.0e-12 | 0.00% |
| ratio | -0.10 Ω | 6.87% | 0.10 Ω | 6.90% |
| ratio ₂ | 0.0 | 0.00% | 3.1e-09 Ω | 0.00% |
| ratio ₁₀ | -0.10 Ω | 7.24% | 0.100 Ω | 7.23% |
| ratio ₁₀₀ | -0.10 Ω | 6.88% | 0.100 Ω | 6.87% |
| ratio _{cm} | 0.0 | 0.00% | 2.2e-09 Ω | 0.00% |
| ratio _{fsl} | -0.10 Ω | 7.43% | 0.10 Ω | 7.45% |
| ratio _{fsl10k} | 0.0 | 0.00% | 2.0e-09 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 2.8e-09 Ω | 0.00% |
| ratio _{pp} | 1.0 Ω | 64.72% | 1.00 Ω | 64.65% |
| ratio _{pph1} | 0.0 | 0.00% | 3.0e-09 Ω | 0.00% |

R_PPH1

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 0.000100 | 19.53% | 0.000100 | 19.51% |
| R ₂ | 0.0 | 0.00% | 6.7e-12 | 0.00% |
| ratio | -0.10 Ω | 19.57% | 0.10 Ω | 19.63% |
| ratio ₂ | 0.0 | 0.00% | 5.1e-09 Ω | 0.00% |
| ratio ₁₀ | -0.10 Ω | 20.61% | 0.100 Ω | 20.57% |
| ratio ₁₀₀ | -0.10 Ω | 19.60% | 0.100 Ω | 19.55% |
| ratio _{cm} | 0.0 | 0.00% | 3.6e-09 Ω | 0.00% |
| ratio _{fsl} | 0.0 | 0.00% | 4.9e-09 Ω | 0.00% |
| ratio _{fsl10k} | 0.0 | 0.00% | 3.3e-09 Ω | 0.00% |
| ratio _{mmln4221} | 0.0 | 0.00% | 4.7e-09 Ω | 0.00% |
| ratio _{pp} | 0.0 | 0.00% | 1.7e-08 Ω | 0.00% |
| ratio _{pph1} | -0.100 Ω | 20.69% | 0.100 Ω | 20.67% |

R_MMLN4221

| Variable | GUM Sensitivity | GUM Proportion | MC Sensitivity | MC Proportion |
|---------------------------|-----------------|----------------|----------------|---------------|
| R | 1.0e-05 | 15.75% | 1.0e-05 | 15.70% |
| R ₂ | 0.0 | 0.00% | 8.3e-14 | 0.00% |
| ratio | -0.010 Ω | 15.79% | 0.010 Ω | 15.80% |
| ratio ₂ | 0.0 | 0.00% | 6.4e-11 Ω | 0.00% |
| ratio ₁₀ | -0.0100 Ω | 16.63% | 0.0100 Ω | 16.56% |
| ratio ₁₀₀ | -0.0100 Ω | 15.82% | 0.0100 Ω | 15.73% |
| ratio _{cm} | 0.0 | 0.00% | 4.5e-11 Ω | 0.00% |
| ratio _{fsl} | -0.0100 Ω | 17.08% | 0.010 Ω | 17.06% |
| ratio _{fsl10k} | 0.0 | 0.00% | 4.1e-11 Ω | 0.00% |
| ratio _{mmln4221} | -0.0100 Ω | 18.93% | 0.0100 Ω | 18.85% |
| ratio _{pp} | 0.0 | 0.00% | 2.1e-10 Ω | 0.00% |
| ratio _{pph1} | 0.0 | 0.00% | 6.2e-11 Ω | 0.00% |

Expanded Uncertainties

GUM Approximation

| Function | Interval | Min | Max | k | Deg. Freedom | Expanded Uncertainty |
|---------------------|----------|---------|---------|-------|----------------|----------------------|
| R _{REF} | 99% | 10000 Ω | 10000 Ω | 2.576 | inf | 0.0017 Ω |
| - | 95% | 10000 Ω | 10000 Ω | 1.960 | inf | 0.0013 Ω |
| - | 68% | 10000 Ω | 10000 Ω | 0.994 | inf | 0.00065 Ω |
| R _{REF2} | 99% | 10000 Ω | 10000 Ω | 2.576 | inf | 0.0013 Ω |
| - | 95% | 10000 Ω | 10000 Ω | 1.960 | inf | 0.00098 Ω |
| - | 68% | 10000 Ω | 10000 Ω | 0.994 | inf | 0.00050 Ω |
| R _{1k} | 99% | 1000 Ω | 1000 Ω | 2.576 | 1305544786.25 | 0.00024 Ω |
| - | 95% | 1000 Ω | 1000 Ω | 1.960 | 1305544786.25 | 0.00018 Ω |
| - | 68% | 1000 Ω | 1000 Ω | 0.994 | 1305544786.25 | 0.000091 Ω |
| R _{1kT2} | 99% | 1000 Ω | 1000 Ω | 2.576 | inf | 0.00021 Ω |
| - | 95% | 1000 Ω | 1000 Ω | 1.960 | inf | 0.00016 Ω |
| - | 68% | 1000 Ω | 1000 Ω | 0.994 | inf | 0.000082 Ω |
| R _{CMDUCK} | 99% | 10000 Ω | 10000 Ω | 2.576 | 122538273.41 | 0.0029 Ω |
| - | 95% | 10000 Ω | 10000 Ω | 1.960 | 122538273.41 | 0.0022 Ω |
| - | 68% | 10000 Ω | 10000 Ω | 0.994 | 122538273.41 | 0.0011 Ω |
| R _{FSL10k} | 99% | 10000 Ω | 10000 Ω | 2.576 | 56585304516.73 | 0.0030 Ω |
| - | 95% | 10000 Ω | 10000 Ω | 1.960 | 56585304516.73 | 0.0023 Ω |
| - | 68% | 10000 Ω | 10000 Ω | 0.994 | 56585304516.73 | 0.0012 Ω |
| R ₁₀₀ | 99% | 100 Ω | 100 Ω | 2.576 | 2408282652.10 | 0.000029 Ω |
| - | 95% | 100 Ω | 100 Ω | 1.960 | 2408282652.10 | 0.000022 Ω |
| - | 68% | 100 Ω | 100 Ω | 0.994 | 2408282652.10 | 0.000011 Ω |
| R ₁₀ | 99% | 10 Ω | 10 Ω | 2.576 | 25179230.33 | 3.4e-06 Ω |
| - | 95% | 10 Ω | 10 Ω | 1.960 | 25179230.33 | 2.6e-06 Ω |
| - | 68% | 10 Ω | 10 Ω | 0.994 | 25179230.33 | 1.3e-06 Ω |
| R _{FSL935} | 99% | 1.0 Ω | 1.0 Ω | 2.576 | 7785363.55 | 3.8e-07 Ω |
| - | 95% | 1.0 Ω | 1.0 Ω | 1.960 | 7785363.55 | 2.9e-07 Ω |
| - | 68% | 1.0 Ω | 1.0 Ω | 0.994 | 7785363.55 | 1.5e-07 Ω |
| R _{PP} | 99% | 1.00 Ω | 1.00 Ω | 2.576 | 8444.55 | 6.4e-07 Ω |
| - | 95% | 1.00 Ω | 1.00 Ω | 1.960 | 8444.55 | 4.9e-07 Ω |
| - | 68% | 1.00 Ω | 1.00 Ω | 0.995 | 8444.55 | 2.5e-07 Ω |
| R _{PPH1} | 99% | 1.00 Ω | 1.00 Ω | 2.576 | 27454495.01 | 3.8e-07 Ω |
| - | 95% | 1.00 Ω | 1.00 Ω | 1.960 | 27454495.01 | 2.9e-07 Ω |
| - | 68% | 1.00 Ω | 1.00 Ω | 0.994 | 27454495.01 | 1.5e-07 Ω |

| Function | Interval | Min | Max | k | Deg. Freedom | Expanded Uncertainty |
|----------------|----------|----------------|----------------|-------|--------------|----------------------|
| $R_{MMLN4221}$ | 99% | 0.100 Ω | 0.100 Ω | 2.576 | 2966861.96 | 4.2e-08 Ω |
| - | 95% | 0.100 Ω | 0.100 Ω | 1.960 | 2966861.96 | 3.2e-08 Ω |
| - | 68% | 0.100 Ω | 0.100 Ω | 0.994 | 2966861.96 | 1.6e-08 Ω |

Monte Carlo

Symmetric Coverage Intervals

| Function | Interval | Min | Max | k |
|----------------|----------|----------------|----------------|-------|
| R_{REF} | 99% | 10000 Ω | 10000 Ω | 2.573 |
| - | 95% | 10000 Ω | 10000 Ω | 1.962 |
| - | 68% | 10000 Ω | 10000 Ω | 0.994 |
| R_{REF2} | 99% | 10000 Ω | 10000 Ω | 2.577 |
| - | 95% | 10000 Ω | 10000 Ω | 1.960 |
| - | 68% | 10000 Ω | 10000 Ω | 0.995 |
| R_{1k} | 99% | 1000 Ω | 1000 Ω | 2.575 |
| - | 95% | 1000 Ω | 1000 Ω | 1.962 |
| - | 68% | 1000 Ω | 1000 Ω | 0.994 |
| R_{1kT2} | 99% | 1000 Ω | 1000 Ω | 2.572 |
| - | 95% | 1000 Ω | 1000 Ω | 1.959 |
| - | 68% | 1000 Ω | 1000 Ω | 0.994 |
| R_{CMDUCK} | 99% | 10000 Ω | 10000 Ω | 2.580 |
| - | 95% | 10000 Ω | 10000 Ω | 1.959 |
| - | 68% | 10000 Ω | 10000 Ω | 0.995 |
| R_{FSL10k} | 99% | 10000 Ω | 10000 Ω | 2.574 |
| - | 95% | 10000 Ω | 10000 Ω | 1.959 |
| - | 68% | 10000 Ω | 10000 Ω | 0.995 |
| R_{100} | 99% | 100 Ω | 100 Ω | 2.576 |
| - | 95% | 100 Ω | 100 Ω | 1.959 |
| - | 68% | 100 Ω | 100 Ω | 0.995 |
| R_{10} | 99% | 10 Ω | 10 Ω | 2.577 |
| - | 95% | 10 Ω | 10 Ω | 1.961 |
| - | 68% | 10 Ω | 10 Ω | 0.994 |
| R_{FSL935} | 99% | 1.0 Ω | 1.0 Ω | 2.574 |
| - | 95% | 1.0 Ω | 1.0 Ω | 1.960 |
| - | 68% | 1.0 Ω | 1.0 Ω | 0.995 |
| R_{PP} | 99% | 1.00 Ω | 1.00 Ω | 2.581 |
| - | 95% | 1.00 Ω | 1.00 Ω | 1.959 |
| - | 68% | 1.00 Ω | 1.00 Ω | 0.995 |
| R_{PPH1} | 99% | 1.00 Ω | 1.00 Ω | 2.577 |
| - | 95% | 1.00 Ω | 1.00 Ω | 1.962 |
| - | 68% | 1.00 Ω | 1.00 Ω | 0.993 |
| $R_{MMLN4221}$ | 99% | 0.100 Ω | 0.100 Ω | 2.574 |
| - | 95% | 0.100 Ω | 0.100 Ω | 1.962 |
| - | 68% | 0.100 Ω | 0.100 Ω | 0.993 |

GUM Derivation

Measurement Model:

$$R_{REF} = R$$

$$R_{REF2} = R_2$$

$$R_{1k} = \frac{R_{REF}}{\text{ratio}}$$

Sensitivity Matrix [Cx]:

| - | R | R ₂ | ratio | ratio ₂ | ratio ₁₀ | ratio ₁₀₀ | ratio _{cm} | ratio _{fsl} | ratio _{fsl10k} | ratio _{mmln4221} | ratio _{pp} | ratio _{pph1} |
|-----------------------|--|--|--|--|---|--|---|--|---|---|---|---|
| R _{REF} | $\frac{\partial}{\partial R} R_{REF}$ | $\frac{\partial}{\partial R_2} R_{REF}$ | $\frac{\partial}{\partial ratio} R_{REF}$ | $\frac{\partial}{\partial ratio_2} R_{REF}$ | $\frac{\partial}{\partial ratio_{10}} R_{REF}$ | $\frac{\partial}{\partial ratio_{100}} R_{REF}$ | $\frac{\partial}{\partial ratio_{cm}} R_{REF}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{REF}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{REF}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{REF}$ | $\frac{\partial}{\partial ratio_{pp}} R_{REF}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{REF}$ |
| R _{REF2} | $\frac{\partial}{\partial R} R_{REF2}$ | $\frac{\partial}{\partial R_2} R_{REF2}$ | $\frac{\partial}{\partial ratio} R_{REF2}$ | $\frac{\partial}{\partial ratio_2} R_{REF2}$ | $\frac{\partial}{\partial ratio_{10}} R_{REF2}$ | $\frac{\partial}{\partial ratio_{100}} R_{REF2}$ | $\frac{\partial}{\partial ratio_{cm}} R_{REF2}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{REF2}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{REF2}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{REF2}$ | $\frac{\partial}{\partial ratio_{pp}} R_{REF2}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{REF2}$ |
| R _{1k} | $\frac{\partial}{\partial R} R_{1k}$ | $\frac{\partial}{\partial R_2} R_{1k}$ | $\frac{\partial}{\partial ratio} R_{1k}$ | $\frac{\partial}{\partial ratio_2} R_{1k}$ | $\frac{\partial}{\partial ratio_{10}} R_{1k}$ | $\frac{\partial}{\partial ratio_{100}} R_{1k}$ | $\frac{\partial}{\partial ratio_{cm}} R_{1k}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{1k}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{1k}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{1k}$ | $\frac{\partial}{\partial ratio_{pp}} R_{1k}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{1k}$ |
| R _{1kT2} | $\frac{\partial}{\partial R} R_{1kT2}$ | $\frac{\partial}{\partial R_2} R_{1kT2}$ | $\frac{\partial}{\partial ratio} R_{1kT2}$ | $\frac{\partial}{\partial ratio_2} R_{1kT2}$ | $\frac{\partial}{\partial ratio_{10}} R_{1kT2}$ | $\frac{\partial}{\partial ratio_{100}} R_{1kT2}$ | $\frac{\partial}{\partial ratio_{cm}} R_{1kT2}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{1kT2}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{1kT2}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{1kT2}$ | $\frac{\partial}{\partial ratio_{pp}} R_{1kT2}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{1kT2}$ |
| R _{CMDUCK} | $\frac{\partial}{\partial R} R_{CMDUCK}$ | $\frac{\partial}{\partial R_2} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_2} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_{10}} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_{100}} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_{cm}} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_{pp}} R_{CMDUCK}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{CMDUCK}$ |
| R _{FSL10k} | $\frac{\partial}{\partial R} R_{FSL10k}$ | $\frac{\partial}{\partial R_2} R_{FSL10k}$ | $\frac{\partial}{\partial ratio} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_2} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_{10}} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_{100}} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_{cm}} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_{pp}} R_{FSL10k}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{FSL10k}$ |
| R ₁₀₀ | $\frac{\partial}{\partial R} R_{100}$ | $\frac{\partial}{\partial R_2} R_{100}$ | $\frac{\partial}{\partial ratio} R_{100}$ | $\frac{\partial}{\partial ratio_2} R_{100}$ | $\frac{\partial}{\partial ratio_{10}} R_{100}$ | $\frac{\partial}{\partial ratio_{100}} R_{100}$ | $\frac{\partial}{\partial ratio_{cm}} R_{100}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{100}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{100}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{100}$ | $\frac{\partial}{\partial ratio_{pp}} R_{100}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{100}$ |
| R ₁₀ | $\frac{\partial}{\partial R} R_{10}$ | $\frac{\partial}{\partial R_2} R_{10}$ | $\frac{\partial}{\partial ratio} R_{10}$ | $\frac{\partial}{\partial ratio_2} R_{10}$ | $\frac{\partial}{\partial ratio_{10}} R_{10}$ | $\frac{\partial}{\partial ratio_{100}} R_{10}$ | $\frac{\partial}{\partial ratio_{cm}} R_{10}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{10}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{10}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{10}$ | $\frac{\partial}{\partial ratio_{pp}} R_{10}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{10}$ |
| R _{FSL935} | $\frac{\partial}{\partial R} R_{FSL935}$ | $\frac{\partial}{\partial R_2} R_{FSL935}$ | $\frac{\partial}{\partial ratio} R_{FSL935}$ | $\frac{\partial}{\partial ratio_2} R_{FSL935}$ | $\frac{\partial}{\partial ratio_{10}} R_{FSL935}$ | $\frac{\partial}{\partial ratio_{100}} R_{FSL935}$ | $\frac{\partial}{\partial ratio_{cm}} R_{FSL935}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{FSL935}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{FSL935}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{FSL935}$ | $\frac{\partial}{\partial ratio_{pp}} R_{FSL935}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{FSL935}$ |
| R _{PP} | $\frac{\partial}{\partial R} R_{PP}$ | $\frac{\partial}{\partial R_2} R_{PP}$ | $\frac{\partial}{\partial ratio} R_{PP}$ | $\frac{\partial}{\partial ratio_2} R_{PP}$ | $\frac{\partial}{\partial ratio_{10}} R_{PP}$ | $\frac{\partial}{\partial ratio_{100}} R_{PP}$ | $\frac{\partial}{\partial ratio_{cm}} R_{PP}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{PP}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{PP}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{PP}$ | $\frac{\partial}{\partial ratio_{pp}} R_{PP}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{PP}$ |
| R _{PPH1} | $\frac{\partial}{\partial R} R_{PPH1}$ | $\frac{\partial}{\partial R_2} R_{PPH1}$ | $\frac{\partial}{\partial ratio} R_{PPH1}$ | $\frac{\partial}{\partial ratio_2} R_{PPH1}$ | $\frac{\partial}{\partial ratio_{10}} R_{PPH1}$ | $\frac{\partial}{\partial ratio_{100}} R_{PPH1}$ | $\frac{\partial}{\partial ratio_{cm}} R_{PPH1}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{PPH1}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{PPH1}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{PPH1}$ | $\frac{\partial}{\partial ratio_{pp}} R_{PPH1}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{PPH1}$ |
| R _{MMLN4221} | $\frac{\partial}{\partial R} R_{MMLN4221}$ | $\frac{\partial}{\partial R_2} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_2} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_{10}} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_{100}} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_{cm}} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_{fsl}} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_{fsl10k}} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_{mmln4221}} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_{pp}} R_{MMLN4221}$ | $\frac{\partial}{\partial ratio_{pph1}} R_{MMLN4221}$ |

| - | R | R ₂ | ratio | ratio ₂ | ratio ₁₀ | ratio ₁₀₀ | ratio _{cm} | ratio _{fsl} | ratio _{fsl10k} | ratio _{mmln4221} | ratio _{pp} | ratio _{pph1} |
|-----------------------|---|-----------------------------------|---|---|---|---|---|---|---|--|--|--|
| R _{REF} | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| R _{REF2} | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| R _{1k} | $\frac{1}{ratio}$ | 0 | $-\frac{R}{ratio^2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| R _{1kT2} | 0 | $\frac{1}{ratio_2}$ | 0 | $-\frac{R_2}{ratio_2^2}$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| R _{CMDUCK} | $\frac{ratio_{cm}}{2ratio}$ | $\frac{ratio_{cm}}{2ratio_2}$ | $-\frac{Rratio_{cm}}{2ratio^2}$ | $-\frac{R_2ratio_{cm}}{2ratio_2^2}$ | 0 | 0 | $\frac{R}{2ratio} + \frac{R_2}{2ratio_2}$ | 0 | 0 | 0 | 0 | 0 |
| R _{FSL10k} | $\frac{ratio_{fsl10k}}{2ratio}$ | $\frac{ratio_{fsl10k}}{2ratio_2}$ | $-\frac{Rratio_{fsl10k}}{2ratio^2}$ | $-\frac{R_2ratio_{fsl10k}}{2ratio_2^2}$ | 0 | 0 | 0 | 0 | $\frac{R}{2ratio} + \frac{R_2}{2ratio_2}$ | 0 | 0 | 0 |
| R ₁₀₀ | $\frac{1}{ratio_{100}}$ | 0 | $-\frac{R}{ratio^2 ratio_{100}}$ | 0 | 0 | $-\frac{R}{ratio_{100}^2}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| R ₁₀ | $\frac{1}{ratio_{10} ratio_{100}}$ | 0 | $-\frac{R}{ratio^2 ratio_{10} ratio_{100}}$ | 0 | $-\frac{R}{ratio_{10}^2 ratio_{100}}$ | $-\frac{R}{ratio_{10} ratio_{100}^2}$ | 0 | 0 | 0 | 0 | 0 | 0 |
| R _{FSL935} | $\frac{1}{ratio_{10} ratio_{100} ratio_{fsl}}$ | 0 | $-\frac{R}{ratio^2 ratio_{10} ratio_{100} ratio_{fsl}}$ | 0 | $-\frac{R}{ratio_{10}^2 ratio_{100} ratio_{fsl}}$ | $-\frac{R}{ratio_{10} ratio_{100}^2 ratio_{fsl}}$ | 0 | $-\frac{R}{ratio_{10} ratio_{100} ratio_{fsl}^2}$ | 0 | 0 | 0 | 0 |
| R _{PP} | $\frac{ratio_{pp}}{ratio_{10} ratio_{100} ratio_{fsl}}$ | 0 | $-\frac{Rratio_{pp}}{ratio^2 ratio_{10} ratio_{100} ratio_{fsl}}$ | 0 | $-\frac{Rratio_{pp}}{ratio_{10}^2 ratio_{100} ratio_{fsl}}$ | $-\frac{Rratio_{pp}}{ratio_{10} ratio_{100}^2 ratio_{fsl}}$ | 0 | $-\frac{Rratio_{pp}}{ratio_{10} ratio_{100} ratio_{fsl}^2}$ | 0 | 0 | $\frac{R}{ratio_{10} ratio_{100} ratio_{fsl}}$ | 0 |
| R _{PPH1} | $\frac{1}{ratio_{10} ratio_{100} ratio_{pph1}}$ | 0 | $-\frac{R}{ratio^2 ratio_{10} ratio_{100} ratio_{pph1}}$ | 0 | $-\frac{R}{ratio_{10}^2 ratio_{100} ratio_{pph1}}$ | $-\frac{R}{ratio_{10} ratio_{100}^2 ratio_{pph1}}$ | 0 | 0 | 0 | 0 | 0 | $-\frac{R}{ratio_{10} ratio_{100} ratio_{pph1}^2}$ |
| R _{MMLN4221} | $\frac{1}{ratio_{10} ratio_{100} ratio_{mmln4221}}$ | 0 | $-\frac{R}{ratio^2 ratio_{10} ratio_{100} ratio_{mmln4221}}$ | 0 | $-\frac{R}{ratio_{10}^2 ratio_{100} ratio_{mmln4221}}$ | $-\frac{R}{ratio_{10} ratio_{100}^2 ratio_{mmln4221}}$ | 0 | $-\frac{R}{ratio_{10} ratio_{100} ratio_{mmln4221}^2}$ | 0 | $-\frac{R}{ratio_{10} ratio_{100} ratio_{mmln4221}}$ | 0 | 0 |

| - | R | R ₂ | ratio | ratio ₂ | ratio ₁₀ | ratio ₁₀₀ | ratio _{cm} | ratio _{fsl} | ratio _{fsl10k} | ratio _{mmln4221} | ratio _{pp} | ratio _{pph1} |
|-----------------------|----------|----------------|----------|--------------------|---------------------|----------------------|---------------------|----------------------|-------------------------|---------------------------|---------------------|-----------------------|
| R _{REF} | 1.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| R _{REF2} | 0.0 | 1.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| R _{1k} | 0.10 | 0.0 | -100 Ω | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| R _{1kT2} | 0.0 | 0.10 | 0.0 | -100 Ω | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| R _{CMDUCK} | 0.50 | 0.50 | -500 Ω | -500 Ω | 0.0 | 0.0 | 1000 Ω | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| R _{FSL10k} | 0.50 | 0.50 | -500 Ω | -500 Ω | 0.0 | 0.0 | 0.0 | 0.0 | 1000 Ω | 0.0 | 0.0 | 0.0 |
| R ₁₀₀ | 0.010 | 0.0 | -10 Ω | 0.0 | 0.0 | -10 Ω | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| R ₁₀ | 0.0010 | 0.0 | -1.0 Ω | 0.0 | -1.0 Ω | -1.0 Ω | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| R _{FSL935} | 0.00010 | 0.0 | -0.10 Ω | 0.0 | -0.10 Ω | -0.10 Ω | 0.0 | -0.10 Ω | 0.0 | 0.0 | 0.0 | 0.0 |
| R _{PP} | 0.000100 | 0.0 | -0.10 Ω | 0.0 | -0.10 Ω | -0.10 Ω | 0.0 | -0.10 Ω | 0.0 | 0.0 | 1.0 Ω | 0.0 |
| R _{PPH1} | 0.000100 | 0.0 | -0.10 Ω | 0.0 | -0.10 Ω | -0.10 Ω | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | -0.100 Ω |
| R _{MMLN4221} | 1.0e-05 | 0.0 | -0.010 Ω | 0.0 | -0.0100 Ω | -0.0100 Ω | 0.0 | -0.0100 Ω | 0.0 | -0.0100 Ω | 0.0 | 0.0 |

Combined Covariance:

$$U_y = C_x \cdot U_x \cdot C_x^T$$

$$V_{RREF} = \frac{v_R u_{RREF}^4}{u_R^4} = \infty$$

$$V_{RREF2} = \frac{v_{R2} u_{RREF2}^4}{u_{R2}^4} = \infty$$

$$V_{R1k} = \frac{u_{R1k}^4}{\frac{R^4 u_{ratio}^4}{v_{ratio}^8} + \frac{u_R^4}{v_R^4}} = 1.306 \cdot 10^9$$

$$V_{R1kT2} = \frac{u_{R1kT2}^4}{\frac{R_2^4 u_{ratio2}^4}{v_{ratio2}^8} + \frac{u_{R2}^4}{v_{R2}^4}} = \infty$$

$$V_{RCMDUCK} = \frac{u_{RCMDUCK}^4}{\frac{R^4 u_{cm}^4 u_{ratio}^4}{16v_{ratio}^8} + \frac{R_2^4 u_{cm}^4 u_{ratio2}^4}{16v_{ratio2}^8} + \frac{u_{ratio_{cm}}^4 \left(\frac{R}{2ratio} + \frac{R_2}{2ratio_2}\right)^4}{v_{ratio_{cm}}} + \frac{ratio_{cm}^4 u_{R2}^4}{16v_{R2}^4} + \frac{ratio_{cm}^4 u_R^4}{16v_R^4}} = 1.225 \cdot 10^8$$

$$V_{RFSL10k} = \frac{u_{RFSL10k}^4}{\frac{R^4 u_{fs10k}^4 u_{ratio}^4}{16v_{ratio}^8} + \frac{R_2^4 u_{fs10k}^4 u_{ratio2}^4}{16v_{ratio2}^8} + \frac{u_{ratio_{fs10k}}^4 \left(\frac{R}{2ratio} + \frac{R_2}{2ratio_2}\right)^4}{v_{ratio_{fs10k}}} + \frac{ratio_{fs10k}^4 u_{R2}^4}{16v_{R2}^4} + \frac{ratio_{fs10k}^4 u_R^4}{16v_R^4}} = 5.659 \cdot 10^{10}$$

$$V_{R100} = \frac{u_{R100}^4}{\frac{R^4 u_{ratio100}^4}{v_{ratio100}^8} + \frac{R^4 u_{ratio}^4}{v_{ratio}^8} + \frac{u_R^4}{v_R^4}} = 2.408 \cdot 10^9$$

$$V_{R10} = \frac{u_{R10}^4}{\frac{R^4 u_{ratio100}^4}{v_{ratio100}^8} + \frac{R^4 u_{ratio10}^4}{v_{ratio10}^8} + \frac{R^4 u_{ratio}^4}{v_{ratio}^8} + \frac{u_R^4}{v_R^4}} = 2.518 \cdot 10^7$$

$$V_{RFSL935} = \frac{u_{RFSL935}^4}{\frac{R^4 u_{ratio_{fsl}}^4}{v_{ratio_{fsl}}^8} + \frac{R^4 u_{ratio100}^4}{v_{ratio100}^8} + \frac{R^4 u_{ratio10}^4}{v_{ratio10}^8} + \frac{R^4 u_{ratio}^4}{v_{ratio}^8} + \frac{u_R^4}{v_R^4}} = 7.785 \cdot 10^6$$

$$V_{RPP} = \frac{u_{RPP}^4}{\frac{R^4 u_{ratio_{pp}}^4}{v_{ratio_{pp}}^8} + \frac{R^4 u_{ratio_{pp}^4} u_{ratio_{fsl}}^4}{v_{ratio_{fsl}}^8} + \frac{R^4 u_{ratio_{pp}^4} u_{ratio100}^4}{v_{ratio100}^8} + \frac{R^4 u_{ratio_{pp}^4} u_{ratio10}^4}{v_{ratio10}^8} + \frac{R^4 u_{ratio_{pp}^4} u_{ratio}^4}{v_{ratio}^8} + \frac{ratio_{pp}^4 u_R^4}{v_R^4}} = 8445.0$$

$$V_{RPPH1} = \frac{u_{RPPH1}^4}{\frac{R^4 u_{ratio_{pph1}}^4}{v_{ratio_{pph1}}^8} + \frac{R^4 u_{ratio100}^4}{v_{ratio100}^8} + \frac{R^4 u_{ratio10}^4}{v_{ratio10}^8} + \frac{R^4 u_{ratio}^4}{v_{ratio}^8} + \frac{u_R^4}{v_R^4}} = 2.745 \cdot 10^7$$

$$V_{RMMLN4221} = \frac{u_{RMMLN4221}^4}{\frac{R^4 u_{ratio_{mm4221}}^4}{v_{ratio_{mm4221}}^8} + \frac{R^4 u_{ratio_{fsl}}^4}{v_{ratio_{fsl}}^8} + \frac{R^4 u_{ratio100}^4}{v_{ratio100}^8} + \frac{R^4 u_{ratio10}^4}{v_{ratio10}^8} + \frac{R^4 u_{ratio}^4}{v_{ratio}^8} + \frac{u_R^4}{v_R^4}} = 2.967 \cdot 10^6$$

GUM Validity

Comparison to Monte Carlo 95.00% Coverage

1 significant digit. $\delta = 0.000050 \Omega$.

R_REF

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 10000.00001 Ω | 10000.00255 Ω |
| MC | 10000.00001 Ω | 10000.00256 Ω |
| abs(GUM - MC) | 5.7e-06 Ω | 6.1e-06 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 0.000050 \Omega$.

R_REF2

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 10000.00032 Ω | 10000.00228 Ω |
| MC | 10000.00032 Ω | 10000.00228 Ω |
| abs(GUM - MC) | 7.0e-07 Ω | 1.3e-06 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 5.0e-06 \Omega$.

R_1k

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 1000.034588 Ω | 1000.034948 Ω |
| MC | 1000.034588 Ω | 1000.034949 Ω |
| abs(GUM - MC) | 7.4e-08 Ω | 9.1e-07 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 5.0e-06 \Omega$.

R_1k_T2

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 1000.034466 Ω | 1000.034788 Ω |
| MC | 1000.034466 Ω | 1000.034788 Ω |
| abs(GUM - MC) | 2.5e-07 Ω | 3.2e-07 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 0.00050 \Omega$.

R_CMDUCK

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 9999.998649 Ω | 10000.00299 Ω |
| MC | 9999.998635 Ω | 10000.00298 Ω |
| abs(GUM - MC) | 0.000014 Ω | 0.000012 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 0.00050 \Omega$.

R_FSL10k

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 9999.972817 Ω | 9999.977443 Ω |
| MC | 9999.972832 Ω | 9999.977457 Ω |
| abs(GUM - MC) | 0.000015 Ω | 0.000014 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 5.0e-06 \Omega$.

R100

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 100.0038556 Ω | 100.0038998 Ω |
| MC | 100.0038555 Ω | 100.0038996 Ω |
| abs(GUM - MC) | 8.4e-08 Ω | 1.3e-07 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 5.0e-07 \Omega$.

R_10

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 10.00059148 Ω | 10.00059662 Ω |
| MC | 10.00059148 Ω | 10.00059662 Ω |
| abs(GUM - MC) | 1.7e-09 Ω | 4.1e-10 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 5.0e-08 \Omega$.

R_FSL935

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|----------------------|----------------------|
| GUM | 1.000063184 Ω | 1.000063762 Ω |
| MC | 1.000063183 Ω | 1.000063762 Ω |
| abs(GUM - MC) | 1.1e-09 Ω | 7.8e-10 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 5.0e-08 \Omega$.

R_PP

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|-----------------------|-----------------------|
| GUM | 0.9999987812 Ω | 0.9999997544 Ω |
| MC | 0.9999987805 Ω | 0.9999997526 Ω |
| abs(GUM - MC) | 7.0e-10 Ω | 1.8e-09 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 5.0e-08 \Omega$.

R_PPH1

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|-----------------------|-----------------------|
| GUM | 0.9999992387 Ω | 0.9999998153 Ω |
| MC | 0.9999992371 Ω | 0.9999998141 Ω |
| abs(GUM - MC) | 1.6e-09 Ω | 1.2e-09 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

1 significant digit. $\delta = 5.0e-09 \Omega$.

R_MMLN4221

| 95.00% Coverage | Lower Limit | Upper Limit |
|--------------------------|------------------------|------------------------|
| GUM | 0.09999673205 Ω | 0.09999679624 Ω |
| MC | 0.09999673178 Ω | 0.09999679611 Ω |
| abs(GUM - MC) | 2.7e-10 Ω | 1.3e-10 Ω |
| abs(GUM - MC) < δ | PASS | PASS |

Monte Carlo Inputs

